

Animals & Scale

Part 1



National Science Foundation
WHERE DISCOVERIES BEGIN

The Croods (2013)

The Croods is a film rich with fantastic, colorful creatures of all different sizes.

A challenge in creating such a world is to have mammals and birds that look and move in a way that's believable.



Size, Area, and Volume

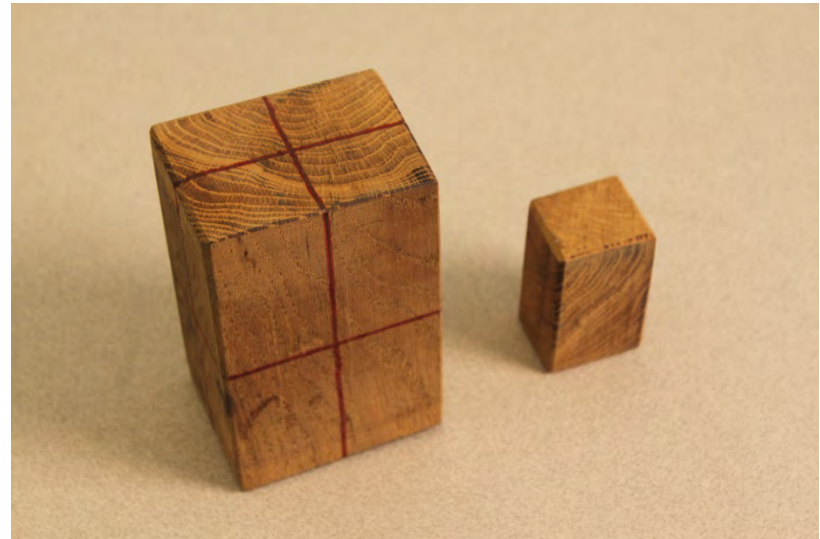
Area goes as:

$$(\text{Size}) \times (\text{Size}) = (\text{Size})^2$$

Volume goes as:

$$(\text{Size}) \times (\text{Size}) \times (\text{Size}) = (\text{Size})^3$$

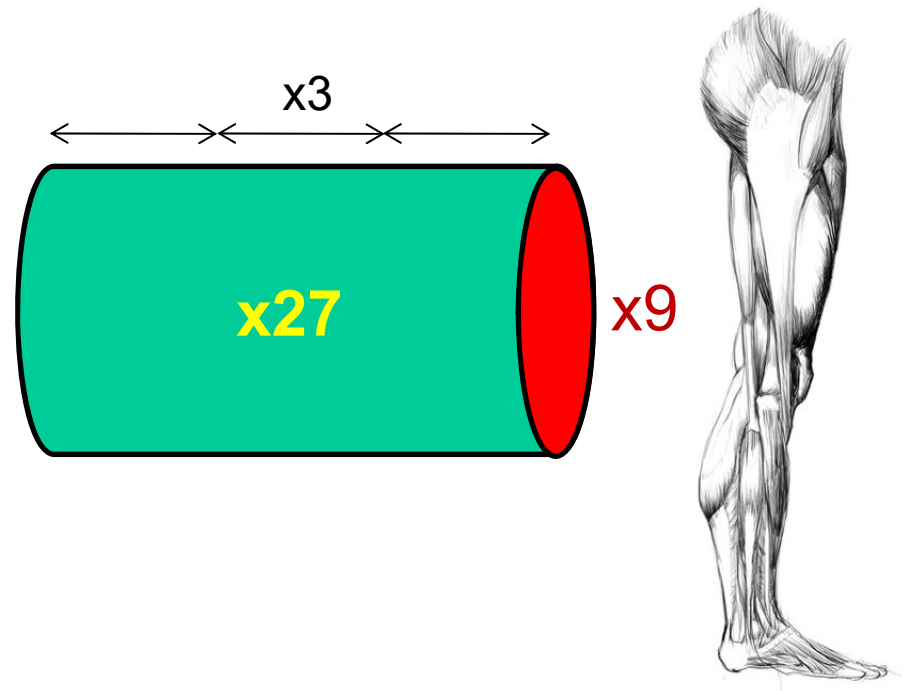
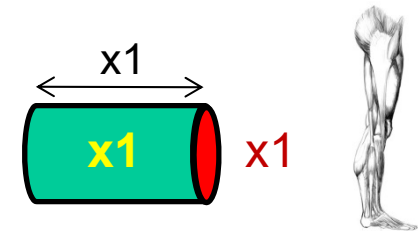
Big cube is 2x the size
so it has 4x the area
and 8x the volume.



Size, Strength, and Weight

Strength scales as area,
Weight scales as volume.

Leg that is x3 in length
has muscles that are
x9 the strength but
with x27 the weight.



Jump Height

Jump height (actual) is **independent** of animal size.

Relative jump height (compared with body size) is a physical cue of size.

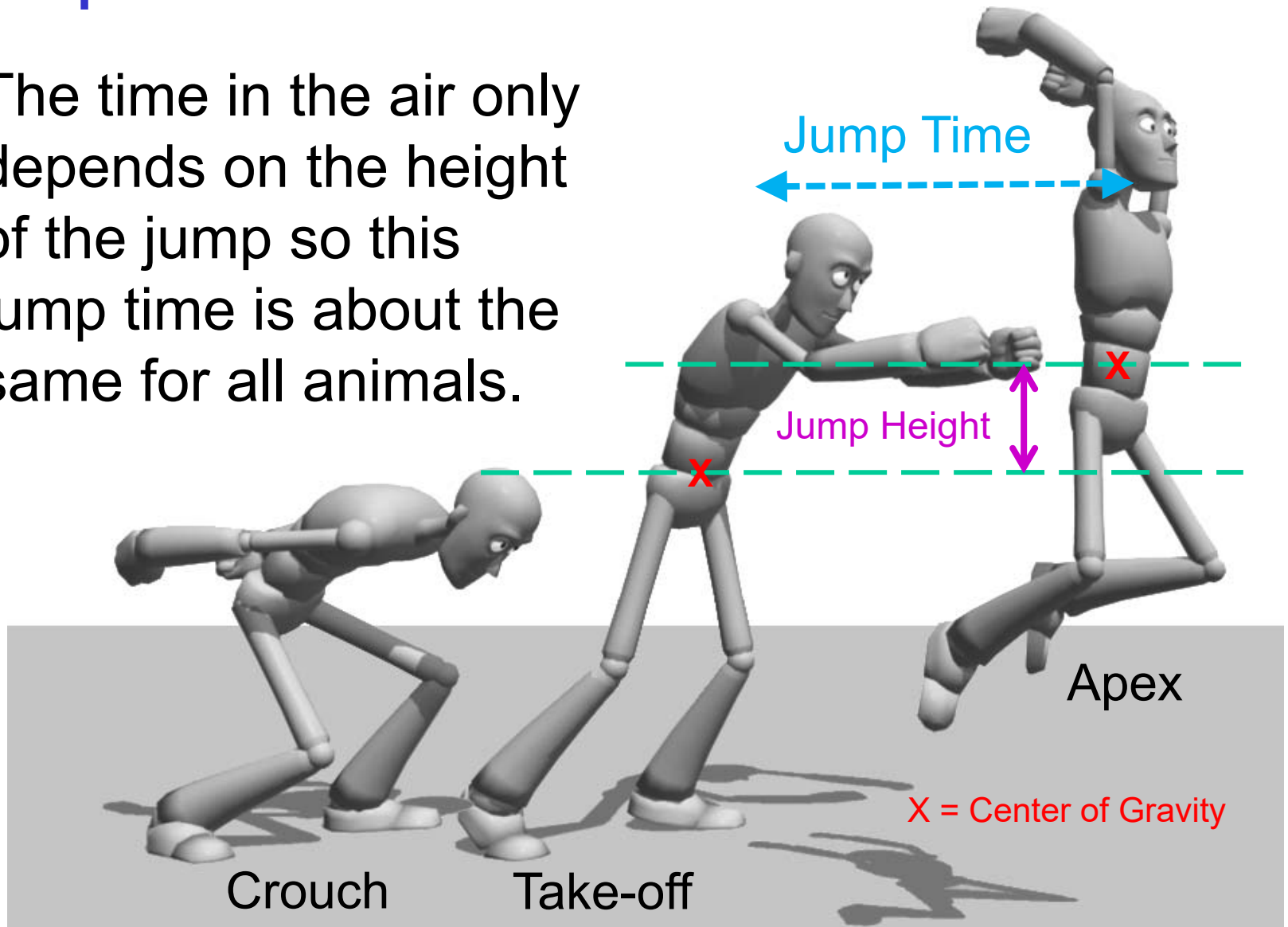
My cat and I can both jump about the height of this pot, which is a third of my body size but about equal to his.

Muscle strength scales as area and leg length scales as body height however body weight scales as volume.



Jump Time

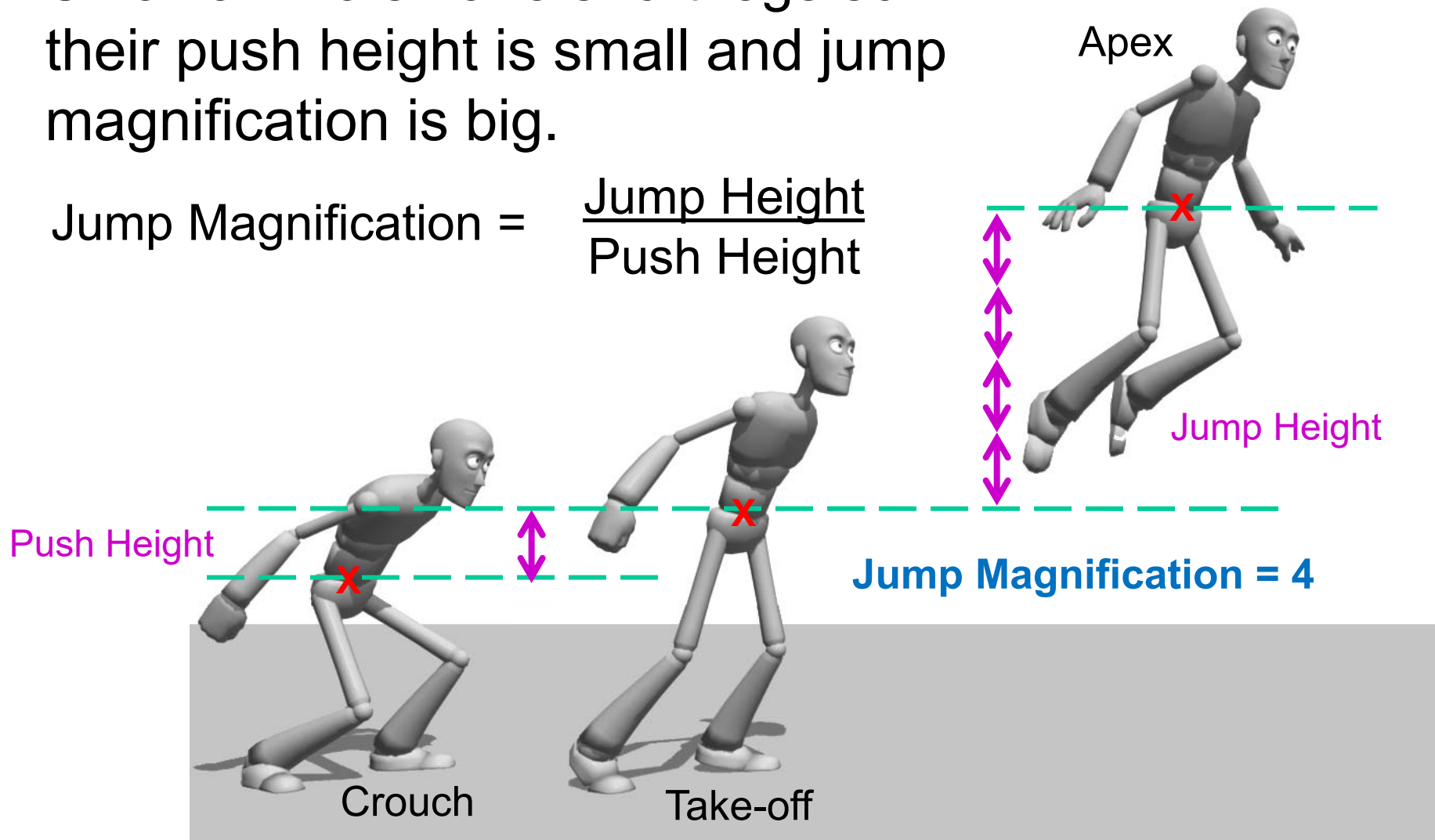
The time in the air only depends on the height of the jump so this jump time is about the same for all animals.



Jump Magnification

Small animals have short legs so their push height is small and jump magnification is big.

$$\text{Jump Magnification} = \frac{\text{Jump Height}}{\text{Push Height}}$$

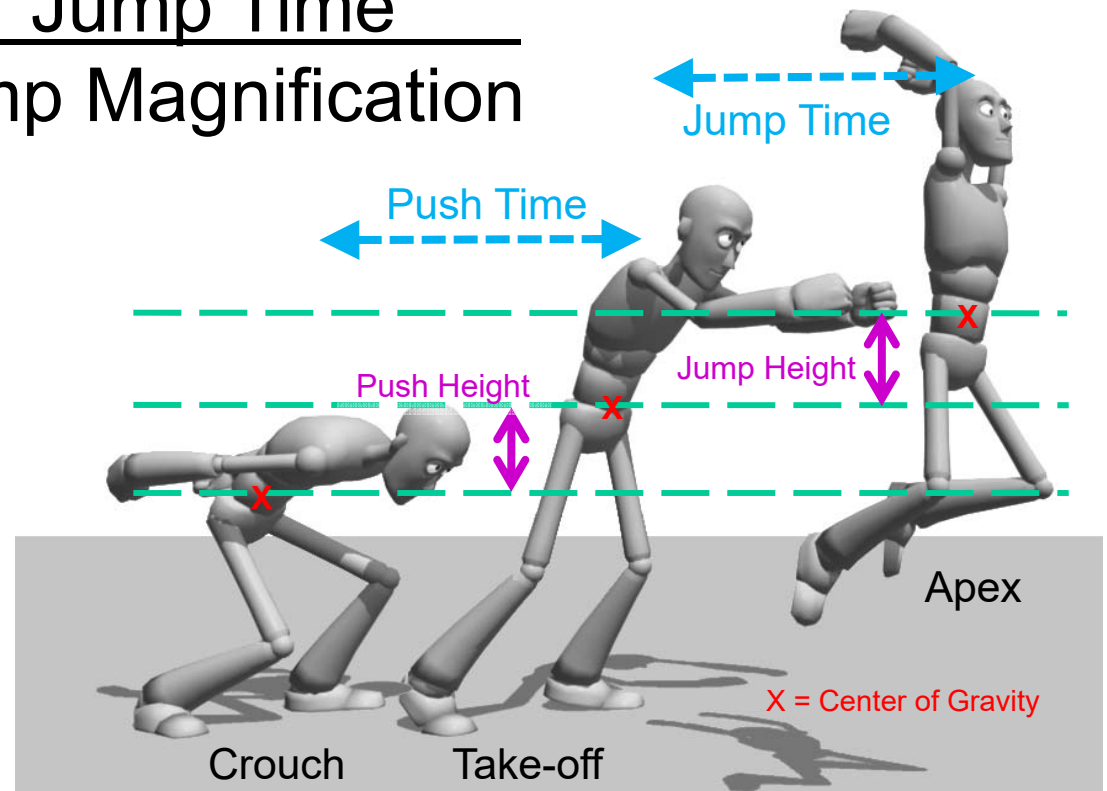


Timing the Push

Small animals jump with a large jump magnification so their push time is short.

$$\text{Push Time} = \frac{\text{Jump Time}}{\text{Jump Magnification}}$$

My cat is a third of my size so his push height and push time are about three times shorter than mine.



Running Speed

Running speed is
independent of
animal size.

Muscle strength
scales as area and
stride length scales
as height however
body weight scales
as volume.

Zebra 40 mph



Rabbit
35 mph



Giraffe
32 mph



Most mammals run between 20 to 50 mph, except the very small or large.

Relative Running Speed

Small animals run fast relative to their size (relative running speed).

Rabbit covers a distance equal to its body length in about $\frac{1}{2}$ frame.



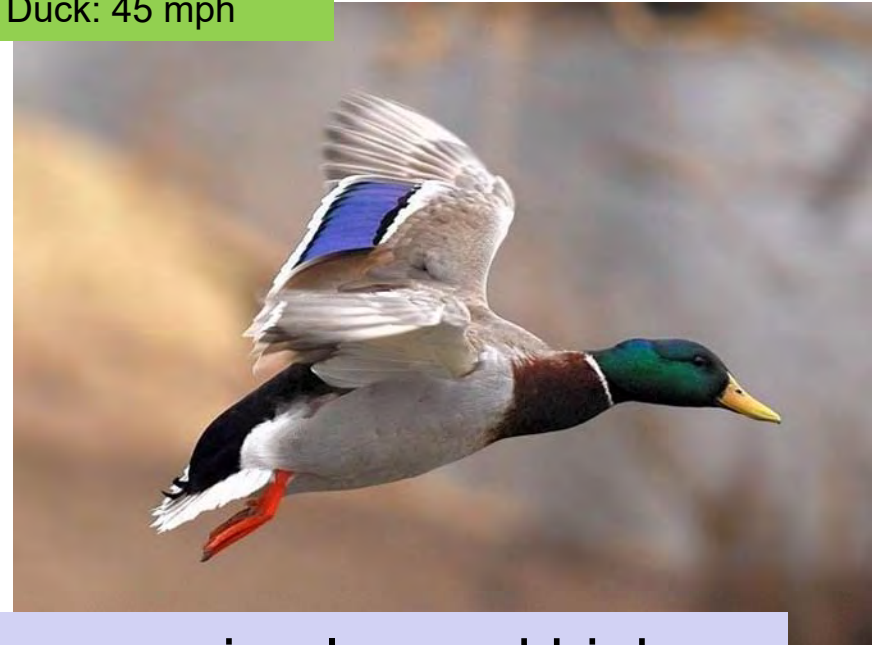
Zebra covers a distance equal to its body length in about 3 frames.

Flying Speed

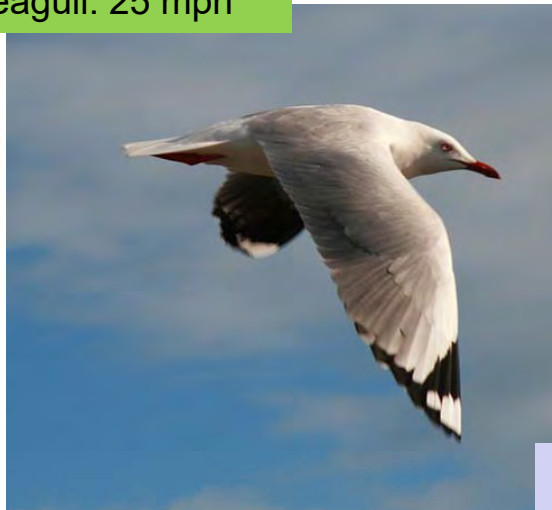
Flying speed is a physical cue for animal size.

Lift force goes as $(\text{area}) \times (\text{velocity})^2$ while weight goes as volume

Duck: 45 mph



Seagull: 25 mph



Sparrow: 15 mph



This is for sustained, cruising flight, not sprinting or diving

Large animals need higher speed to generate enough lift to sustain their weight.

Wing Size & Shape

Wing size and shape is a physical cue for animal size.

Lift force varies with area and wing shape

Short, stubby wings provide less lift but are more maneuverable.

Sparrow: Short, stubby wings



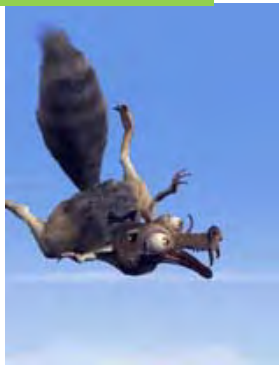
Canada Goose: Large, narrow wings

Terminal Velocity

Maximum falling speed (terminal velocity) is a physical cue for size.

Weight goes as volume but force of air resistance goes as $(\text{area}) \times (\text{speed})^2$

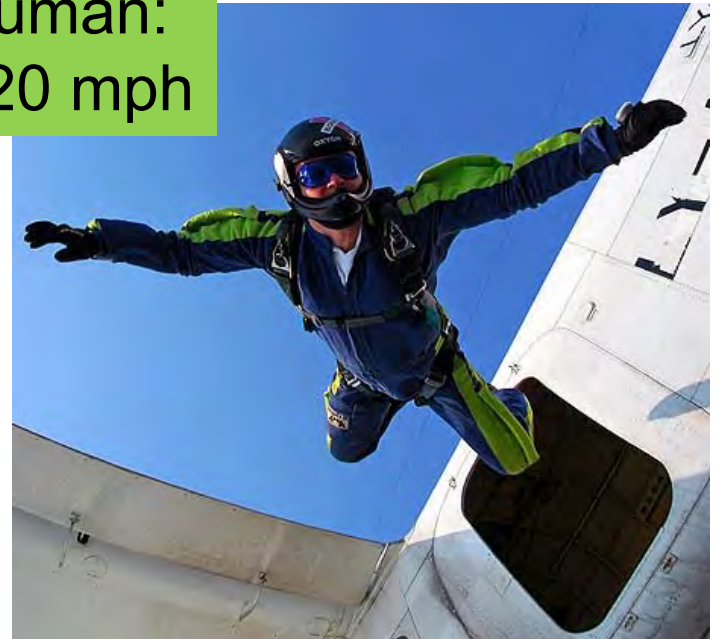
Squirrel:
25 mph



Cat: 50 mph



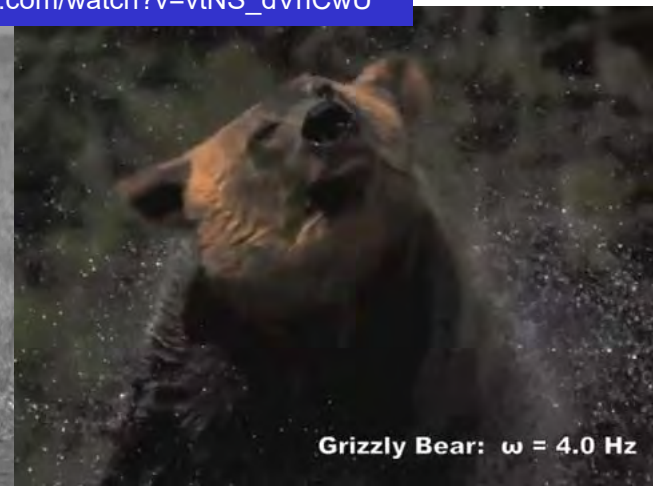
Human:
120 mph



Shake Timing

Timing of an animal's shake is a physical cue for size.

Rotational inertia increases faster than volume but muscle force goes as area



http://www.youtube.com/watch?v=vtNS_dVhCwU

When they dry off small animals will shake with a rapid (high frequency) oscillation.

Summary

- Jump height and jump time (time in the air) is similar for all animals.
- Small animals have a short push height, large jump magnification, and short push time.
- Actual running speed is similar for all mammals.
- Small mammals run fast, relative to their size.
- Large birds fly faster than small birds and also need proportionally larger wings.
- Large animals fall faster than small ones.
- Small animals shake faster than large ones.